

# **FOUNDATIONS & PRE-CALCULUS 10**

## **Seminar Notes** **Learning Guides 15 & 16**

**SYSTEM OF  
EQUATIONS**

## Topic 1

# Developing Systems of Linear Equations

### Example 1 Using a Diagram to Model a Situation

- a) Create a linear system to model this situation:  
The perimeter of a Nunavut flag is 16 ft.  
Its length is 2 ft. longer than its width.



- b) Denise has determined that the Nunavut flag is 5 ft. long and 3 ft. wide.  
Use the linear system from part a to verify that Denise is correct.

#### CHECK YOUR UNDERSTANDING

- Try:** a) Create a linear system to model this situation:  
The stage at the Lyle Victor Albert Centre in Bonnyville, Alberta, is rectangular. Its perimeter is 158 ft. The width of the stage is 31 ft. less than the length.
- b) Sebi has determined that the stage is 55 ft. long and 24 ft. wide. Use the linear system from part a to verify that Sebi is correct.

### Example 2 Using a Table to Create a Linear System to Model a Situation

- a) Create a linear system to model this situation:  
In Calgary, a school raised \$195 by collecting 3000 items for recycling.  
The school received 5¢ for each pop can and 20¢ for each large plastic bottle.
- b) The school collected 2700 pop cans and 300 plastic bottles.  
Use the linear system to verify these numbers.

#### CHECK YOUR UNDERSTANDING

- Try:** a) Create a linear system to model this situation:  
A school raised \$140 by collecting 2000 cans and glass bottles for recycling.  
The school received 5¢ for a can and 10¢ for a bottle.
- b) The school collected 1200 cans and 800 bottles.  
Use the linear system to verify these numbers.

## Topic 2

# Solving a System of Linear Equations Graphically

### Example 1 Solving a Linear System by Graphing

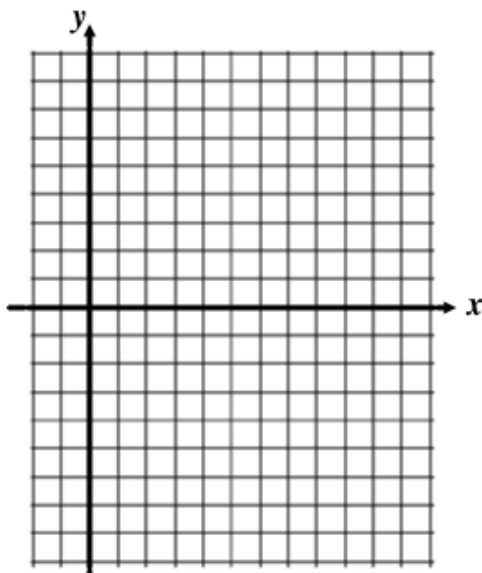
Solve this linear system.

$$x + y = 8$$

$$3x - 2y = 14$$

**1<sup>st</sup> Step:** Get into Slope-Intercept Form  $y = mx + b$

**2<sup>nd</sup> Step:** Then Graph using  $m$  &  $b$

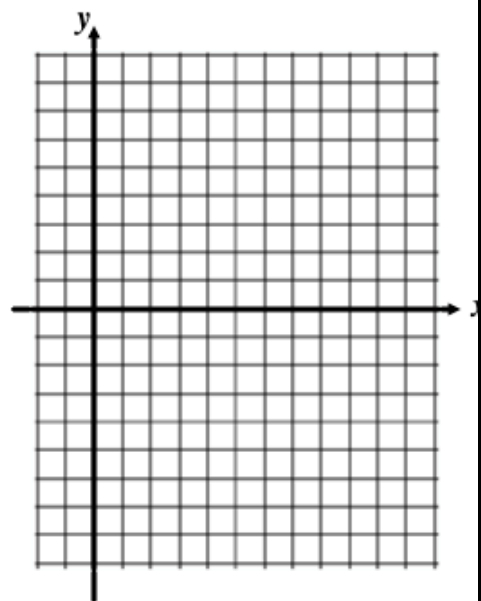


### CHECK YOUR UNDERSTANDING

**Try:** Solve this linear system.

$$2x + 3y = 3$$

$$x - y = 4$$



### Example 3 Solving a Problem by Writing then Graphing a Linear System

a) Write a linear system to model this situation:

To visit the Head-Smashed-In Buffalo Jump interpretive centre near Fort Macleod, Alberta, the admission fee is \$5 for a student and \$9 for an adult. In one hour, 32 people entered the centre and a total of \$180 in admission fees was collected.

b) Graph the linear system then solve this problem: How many students and how many adults visited the centre during this time?

# LEARNING GUIDE 16

## Topic 3

## Using a Substitution Strategy to Solve a System of Linear Equations

### Example 1 Solving a Linear System by Substitution

Solve this linear system.

$$2x - 4y = 7$$

$$4x + y = 5$$

### CHECK YOUR UNDERSTANDING

**Try:** Solve this linear system.

$$5x - 3y = 18$$

$$4x - 6y = 18$$

### Example 2 Using a Linear System to Solve a Problem

a) Create a linear system to model this situation:

Nuri invested \$2000, part at an annual interest rate of 8% and the rest at an annual interest rate of 10%. After one year, the total interest was \$190.

b) Solve this problem: How much money did Nuri invest at each rate?

## Topic 4

# Using an Elimination Strategy to Solve a System of Linear Equations

### Example 1 Solving a Linear System by Subtracting to Eliminate a Variable

Solve this linear system by elimination.

$$3x - 4y = 7$$

$$5x - 6y = 8$$

#### CHECK YOUR UNDERSTANDING

**Try:** Solve this linear system by elimination.

$$2x + 7y = 24$$

$$3x - 2y = -4$$

### Example 2 Solving a Linear System by Adding to Eliminate a Variable

Use an elimination strategy to solve this linear system.

$$\frac{2}{3}x - \frac{1}{2}y = 4$$

$$\frac{1}{2}x + \frac{1}{4}y = \frac{5}{2}$$

#### CHECK YOUR UNDERSTANDING

**Try:** Use an elimination strategy to solve this linear system.

$$\frac{3}{4}x - y = 2$$

$$\frac{1}{8}x + \frac{1}{4}y = 2$$

### Example 3

### Using a Linear System to Solve a Problem

- a) Write a linear system to model this situation:

An alloy is a mixture of metals. An artist was commissioned to make a 100-g bracelet with a 50% silver alloy. He has a 60% silver alloy and a 35% silver alloy.

- b) Solve this problem:

What is the mass of each alloy needed to produce the desired alloy?

#### CHECK YOUR UNDERSTANDING

- Try:** a) Write a linear system to model this situation:  
An artist was commissioned to make a 625-g statue of a raven with a 40% silver alloy. She has a 50% silver alloy and a 25% silver alloy.
- b) Solve this problem: What is the mass of each alloy needed to produce the desired alloy?